

note that we are not able to give arcs in arc order at the same time. The keyword NETWORK in the PERIODS header indicates that the problem is a pure network.

Time file - example.

TIME PERIODS	problem name
NODE1	PERIOD1
NODE3	PERIOD2
NODE7	PERIOD3

ENDATA

In the example, NODE1 and NODE2 are first period nodes, NODE3 to NODE6 are second period nodes, and all remaining nodes are third period nodes. Arcs going from first to second period nodes are a part of the first period decisions, and carry flow over to the second period by defining external flows for that period.

3.3 Stoch File

Since arcs are defined by pairs of nodes, to say that the cost of the arc from node NODE1 to node NODE2 is random requires three parameters. The same goes for bounds and multipliers. We can use the CODE field for that purpose as in the following example. (The data line format used in the stoch file for the networks case is the same as that for the LP case.)

INDEP	DISCRETE	NETWORK
C1 NODE1	NODE3	6.0
C1 NODE1	NODE5	8.0
U2 NODE6	NODE3	8.0
U2 NODE6	NODE5	7.0
SU NODE6	NODE8	9.0
SU NODE6	NODE2	6.0
SU NODE6	NODE2	8.0

PERIOD2 0.6
PERIOD2 0.4
PERIOD2 0.2
PERIOD2 0.8
PERIOD2 0.1
PERIOD2 0.9

The keyword NETWORK indicates that there is something to look for in the code field of the subsequent data records. We use C1 for "cost of first arc from node NODE1 to node NODE2" and use higher numbers, such as C2, for the second parallel arc, etc. Similarly, M = multiplier, U = upper bound, and L = lower bound. Random supply and demand are accommodated by use of SU and DE, respectively, in the code fields as illustrated. This format can be changed to all the other distribution forms in obvious ways.

4. Coupled LP and Network Formats

A network can be viewed as a special case of a linear program, yet it is desirable to use the more compact network data format to express those parts of a multistage problem that may be interpreted as network flow problems. The nodes of a network flow problem are the rows in its LP statement. Our proposal for the coupled format utilizes an MPSX-like format, but uses the ARCS card to indicate that the following data lines are in the NETGEN format and the COLUMNS card to indicate that the

following lines are in MPSX format. While this is consistent with the philosophy as expressed in the introduction, it does have a particular disadvantage. Many multi-stage mixed LP/network problems will actually be composed from separate problem files. To generate the proposed format will involve a certain amount of editing of these files, however this editing could be automated in various (system specific) ways.

The first section is the ROWS. (The absence of a ROWS card tells the program that the problem to follow is a pure network.) Note that only those node names that are going to appear as row names of an LP variable need to be named in the ROWS section. Then follows the COLUMNS/ARCS section. Once the data for the columns and arcs has been entered, then the other sections (RHS, BOUNDS, SUPPLY, etc.) may follow. With the proper logic, the same computer program can read all three formats and does not need to be told beforehand the nature of the problem in the file, whether pure LP, pure network, or mixed. As always, the end of the problem is indicated by an ENDDATA line. Below is an example for the case when we first have LP, then networks and then LP again.

Core file - example of coupled format

NAME ROWS	problem name
-----------	--------------

E	ROW3					
E	ROW4					
L	NODE1					
G	NODE2					
E	ROW5					
E	ROW6					
.....						
E	ROW3					
E	COL16	value				
	COL17	value				
ARCS						
	NODE1	NODE2	cost	upper	lower	multiplier
	NODE1	NODE7	cost	upper	lower	multiplier

	NODE8	ROW5	cost	upper	lower	multiplier
	NODE8	ROW6	cost	upper	lower	multiplier
COLUMNS						
	COL18	ROW5	value	ROW7	value	
	COL19	ROW6	value	ROW8	value	
RHS	
SUPPLY	
ENDDATA	

If we now have a TIME file as follows, the coupling is done.

Time file

```

TIME          problem name
PERIODS      MIXED
COL1         ROW1           PERIOD1
COL6         ROW3           PERIOD2
                  NODE1          PERIOD3
                  NODE3          PERIOD4
COL18        ROW5           PERIOD5
                  NODE6          PERIOD6
ENDATA

```

That the problem is a mixed LP/network is indicated by the keyword MIXED. Here we have that COL1 through COL5 are first stage decision variables, with ROW1 and ROW2 first stage constraints. COL6 through COL17 are second stage decision variables, with ROW3 and ROW4 as constraints. Arcs originating in NODE1 and NODE2 are third stage decision variables, arcs originating in nodes NODE3 through NODE8 belong to stage 4. Finally, all variables corresponding to columns COL18 through whatever the second COLUMNNS section dictates are fifth stage decisions with all constraints after ROW5 associated with them.

The last two entries in the first COLUMNNS section will take values from the second to the third stage. The amount will be determined by the values of COL16 and COL17 and the corresponding entries in this COLUMNNS section.

The last two entries in the ARCS section will bring "flow" from NODE8 to the right hand side of ROW5 and ROW6 by entering a number in those rows. The number will be the "multiplier" from the input, and the value ending up on the right hand side will be the product of this multiplier and the flow running out of NODE8 to these rows (which are nodes when viewed from the network).

Acknowledgements

The authors are grateful to Dalhousie University and the Natural Sciences and Engineering Research Council of Canada for providing facilities and support for this research.

References

- [1] J.R. Birge, "Decomposition and partitioning methods for multistage stochastic linear programs", *Operations Research* 33(1985), 989-1007.
- [2] J.R. Birge and R. J-B Wets, "A sublinear approximation method for stochastic programming", Department of Industrial and Operations Engineering, The University of Michigan, Technical Report 86-26.
- [3] G. Dantzig, *Linear Programming and Extensions*, Princeton University Press, 1968.

Core file sections for networks

1. NAME – starts the input file. The rest of the line can be used for the problem name.
2. ARCS section – each data line following the ARCS header specifies input for one arc. In the first name field is the name of the originating node for the arc, in the second name field the name of the terminating node, in the first numeric field the unit cost, in the second numeric field the upper bound on arc flow, in the third numeric field the lower bound on the flow (if not zero) and in the fourth numeric field the arc multiplier (arc gain) if we are dealing with generalized networks. If the word UNCAP follows the ARCS code, upper and lower bounds need not be specified as they are assumed to be ∞ and zero, respectively. Similarly, the keyword UNDIR signals an undirected network with default bounds of $+\infty$ and $-\infty$.
3. SUPPLY (optional) – each data line following the SUPPLY header contains a node name in the first name field and the amount supplied in the second numeric field.
4. DEMAND (optional) – each data line following the DEMAND header contains a node name in the first name field and the amount demanded in the second numeric field.
5. ENDATA – informative. End of problem data.

Note that there is no section naming all nodes (i.e., rows). They are named implicitly by their appearance in the ARCS section. Also note that arcs (i.e., columns) have no names. Hence they cannot be referred to by name, only by a pair of node names. However, if there are parallel arcs, the user must be careful.

Core file – example

NAME	problem name
ARCS	
NODE1	NODE2 cost
NODE1	NODE3 cost
.....
NODEk	NODEn cost
SUPPLY
NODE1
DEMAND

ENDATA

3.2 Time File

It is normally assumed that in a NETGEN file, all arcs originating in a given node are given before we start giving arcs originating in the next node. This rule should be followed. We shall further assume that FROM-nodes are given in node order, in the sense that if the arcs originating in NODEi occur before those originating in NODEj, then NODEj belongs to the same or a later time period. However,

Scenarios – example

		DISCRETE	
SCENARIOS	ROOT	0.5	PERIOD1
SC SCEN1	ROW2	1.0	
COL1	ROW3	1.0	
COL2	ROW4	1.0	
COL3	ROW5	1.0	
COL4	SCEN2	0.2	PERIOD3
SC SCEN3	SCEN1	0.2	
COL4	ROW5	0.0	PERIOD4
SC SCEN4	SCEN1	0.1	PERIOD2
COL2	ROW3	0.0	
COL3	ROW4	0.0	
COL4	ROW5	0.0	

This is a description of the distribution of four entries: COL1/ROW2, COL2/ROW3, COL3/ROW4, COL4/ROW5, which for convenience we denote here as d_1, d_2, d_3, d_4 , respectively (see Figure 2). Note that in PERIOD4 there are two nodes for the “state” $d_4 = 0.0$ and two for $d_4 = 1.0$, and similarly in PERIOD3 two nodes for $d_3 = 1.0$. This is because a node is distinguished by the information that one has collected concerning the path up to and including time t . Thus in PERIOD3 the two nodes are distinguished because in scenario SCEN1 one knows that the final state is $d_4 = 1.0$, whereas in SCEN2 the outcome of d_4 is in doubt.

3. Network Standard Format

There are several network formats in use. However, it is our view that the most common format is the NETGEN format, see Klingman, Napier and Stutz [10]. For NETGEN we have the following organization of the data line.

Data line for networks

- columns 2–4: code field
- columns 7–12: first name field
- columns 13–18: second name field
- columns 21–30: first numeric field
- columns 31–40: second numeric field
- columns 41–50: third numeric field
- columns 51–60: fourth numeric field

3.1 Core File

As in MPSX there are header lines and data lines in the input format. We adopt a slight variation of the NETGEN standard in omitting the BEGIN line and substituting a NAME line to start the input file and in changing the END line to ENDATA.

[4] J. Edwards, J. Birge, A. King and L. Nazareth, “A standard input format for computer codes which solve stochastic programs with recourse and a library of utilities to simplify its use”, International Institute for Applied Systems Analysis, Working Paper WP-85-03, 1985.

[5] Yu. Ermolieva and R.J-B. Wets, *Numerical Methods for Stochastic Programming*, Springer Verlag, 1987.

[6] International Business Machines, Inc., *Mathematical Programming Subsystem – Extended (MPSX) and Generalized Upper Bounding (GUB) Program Description*, document number SH20-0968-1, 1972.

[7] International Business Machines, Inc., *Mathematical Programming Subsystem – Extended (MPSX) and Mixed Integer Programming (MIP) Program Description*, document number GH19-1091-0.

[8] N.L. Johnson and S. Kotz, *Distributions in Statistics*, Vol. 4, Wiley, New York, 1972.

[9] A.J. King, “Stochastic programming problems: examples from the literature”, in Yu. Ermolieva and R.J-B. Wets, *op cit.*

[10] D. Klingman, A. Napier and J. Stutz, “NETGEN: A program for generating large scale capacitated assignment, transportation, and minimum cost flow network problems”, *Management Science* 20(1974), 814–821.

[11] M. Lane and P. Hutchinson, “A model for managing a certificate of deposit portfolio under uncertainty”, in: *Stochastic Programming*, M.A.H. Dempster, ed., Academic Press, 1980.

[12] B.A. Murtagh and M.A. Saunders, “MINOS – User’s Guide”, Technical Report SOL 77-9, Systems Optimization Laboratory, Department of O.R., Stanford Univ.

[13] A. Prékopa and T. Szántai, “A new multivariate gamma distribution and its fitting to empirical data”, *Water Resources Research* 14 (1978), 19–24.

[14] A. Prékopa and R.J-B. Wets, *Stochastic Programming: 1984*, Math. Program Study 27, 1986.

[15] H. Raiffa, *Decision Analysis: Introductory Lectures on Choices Under Uncertainty*, Addison-Wesley, Reading, 1968.

[16] H. Raiffa and R. Schlaifer, *Applied Statistical Decision Theory*, Harvard University Press, Cambridge, 1961.

[17] R.J-B. Wets, “Solving stochastic programs with simple recourse, II”, in: Proceedings of 1975 Conference on Information Sciences and Systems, Johns Hopkins Univ. Press, Baltimore, Maryland, 1975.

by Nicholas Beaumont
Monash University
Clayton, Vic. 3168, Australia

1. INTRODUCTION

In some mathematical programming problems binary variables (hereafter called logical variables) are introduced to express logical relationships amongst constraints (see Williams 1978, p.159). The commonest example is either a setup cost being incurred or production being zero. The resulting MIP problem is usually solved by relaxing the MIP problem and forming a tree based on the arbitration of the logical variables - the Branch and Bound algorithm.

This method has a number of disadvantages:

1. Matrix generation is complicated by the need to re-express logical relationships in terms of logical variables and "simple" constraints.
2. It enlarges the problem by introducing extra rows, columns and coefficients.
3. It seems inelegant to express, e.g. a binary disjunction of constraints as two rows knowing that in any integer feasible solution at least one of the rows will be slack.

These considerations lead to a re-examination of the idea (Rado 1966) of arbitrating logical constraints (a "logical constraint" is a logical combination of "simple" constraints) instead of logical variables. For brevity only disjunctions of constraints will be discussed, that is groups of constraints of which at least one must be true.

2. THE ALGORITHM

2.1 The Surrogate

The relaxation of the condition $\delta = 0 \text{ OR } \delta = 1$ is $0 < \delta < 1$. We define a surrogate of a disjunction as a simple constraint which is implied by the variables' bounds and any term of the disjunction. We can then relax a disjunctive programming (DP) problem by replacing each disjunction by a surrogate.

A surrogate for the logical condition that at least k of the m constraints

$$\sum_{j=1}^n a_{ij}x_j < b_i \quad i \in M = \{1, 2, \dots, m\} \quad (1)$$

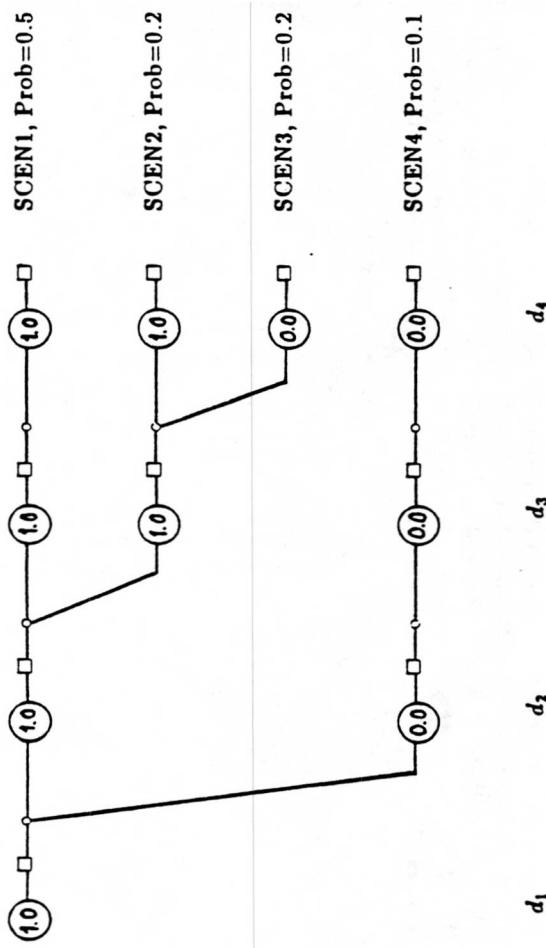


Figure 2. Scenarios example – event tree

is a single "scenario". The nodes visited by the path correspond to certain values assumed by certain entries of the matrices in the core file. Thus a scenario is completely specified by a list of column/row names and values, and a probability value. Once a single given scenario is described, then other scenarios that branch from it may be described by indicating in which period the branch has occurred, and then listing the subsequent column/row names and values. It is best to work through the example of Figure 2.

There are two types of data lines. The first, signified by SC in the code field, gives the name of the scenario in the first name field and its probability in the first numeric field; and then gives the name of the scenario from which the branch occurred and the name of the period in which the branch occurred—i.e., the first period in which the two scenarios differ—in the second name field and third name field, respectively. A scenario that originates in period one is indicated by ROOT in the name field. The next data lines give the column/row values assumed by the scenario.

all $t = 0, \dots, T - 1$ (with $\mathcal{F}_0 := \{\Omega, \emptyset\}$). Given the process distribution P over the space of trajectories and an event A in period $t + 1$ we may compute the conditional probability $P\{\varphi_{t+1} \in A \mid \mathcal{F}_t\}$. Conversely, these conditional probabilities may be composed to generate the finite dimensional distributions of the process φ . In the case under consideration in this paper, all this may be given a much simpler, more graphic, characterization.

To describe the process paths in the discrete state case, note that φ_t can assume only finitely many values for each t . A given history of values φ_s , for $s = 1, \dots, t$, may be followed by a finite collection of values of φ_{t+1} . We think of these as nodes in period $t + 1$. Following Lane and Hutchinson [11] and Raiffa [15], we construct an event tree representation of the trajectories. Represent the (unique) value of φ_1 by a single node connected by oriented arcs from φ_1 to nodes representing the values of φ_2 . These are the descendant nodes of the first period node in the terminology of Blige [1]. Each node of period 2 is connected to its descendant nodes at period 3 by individual arcs oriented in the direction of the period 3 nodes. This construction is continued by connecting each ancestor at period $t - 1$ with its descendants at period t . Each node of this tree has a single entering arc and multiple departing arcs representing the possible next period events.

A trajectory φ thus corresponds to a path from the period 1 node to a single period T node composed of arcs oriented in the direction of increasing time t and, moreover, corresponds uniquely to a single node in the last period T . There are only finitely many paths linking nodes in period 1 to nodes in period T and to specify the distribution on the paths one needs only to attach a definite probability to each path. Hence specifying the process distribution in terms of path probabilities can be effected in this context by assigning probabilities to period T nodes of the event tree (see Figure 2).

For each period $t = 1, \dots, T$, the corresponding sigma algebra \mathcal{F}_t is formed by taking all possible unions of the events represented by the nodes of period t ; thus the topology of this event tree represents the information about the process expressed by the filtration $\{\mathcal{F}_t : t = 1, \dots, T\}$. To each arc we attach the probability that the terminal node occurs given the initial node has occurred—that is, the conditional probability of φ_{t+1} given the history φ_s for $s = 1, \dots, t$. These arc probabilities can be computed from the path probabilities by summing the probabilities of the paths visiting the terminal node and then dividing by the sum of the probabilities of the paths visiting the initial node. Conversely, if to each arc in the tree we know the conditional probability that its terminal node occurs given that its initial node has occurred, then the probability of any given path is simply the product of the arc probabilities along the path.

A decision z_t is made only on the basis of information collected up to and including time t . This is represented by a single node in period t . The uncertainty faced by the decision maker is represented by the collection of paths that branch from this node. Thus in Figure 2, the decisions occur at the nodes and the scenarios branch after the node.

In a language more specific to our application, a "path" in the tree analogy

must hold is

$$\sum_{j=1}^m (a_{ij}x_j - b_i)/u_i \leq n - k$$

where

$$u_i = \sum_{j=1}^n a_{ij}^{+}x_j - b_i \quad 1 \leq i \leq m \quad (\text{assumed to be positive})$$

$$y^+ \stackrel{\text{def}}{=} \max(y, 0) \quad \text{and} \\ 0 < x_j < u_j \quad j = 1, 2, \dots, n.$$

There is no guarantee that this surrogate will be "efficient", in the sense of being a good approximation to a facet of the convex hull of the feasible area. Sherali and Shetty (1980) give a much fuller discussion of the problem of finding efficient surrogates.

A useful feature is illustrated by the disjunction $x = 0$ or $x > 100$ where $0 < x < 200$. The surrogate is $0 < x < 200$ which means that the surrogate and the terms of the disjunction can all be stored as bounds. No rows or coefficients are required whereas the conventional approach would entail two matrix rows and six coefficients.

2.2 The Disjunctive Algorithm

The following algorithm solves disjunctive programming problems. Note that each aspect of this algorithm has an analogue in the conventional Branch and Bound algorithm.

Step 0 Form the relaxation of the original (maximization) problem by replacing each disjunction by a surrogate. U , the set of unresolved problems, initially comprises this problem alone. Set $BEST = -\infty$.

DO STEPS 1, 2 AND 3 UNTIL U IS empty.

Step 1 Remove a problem from U and solve it as a linear programming problem, denoting its objective function value by z . If this problem is infeasible, set $z = -\infty$.

Step 2 If $z > BEST$, and this is a disjunctive solution, set $BEST = z$ and store the solution.

Step 3 If $z > BEST$, and this is not a disjunctive solution, choose a disjunction which is not satisfied by the current solution. Add to U those problems formed by replacing the surrogate of the chosen disjunction by each term of the disjunction.

Step 4 The optimal feasible solution is the last solution stored in Step 2. If no solution has been stored, the problem is infeasible.

3. CRITERIA

As in the conventional algorithm the total number of nodes which have to be examined is much affected by the way in which the tree is built and traversed. The questions arising in the disjunctive approach are:-

1. Which problem to select from the set of unresolved problems.
2. Which disjunction to arbitrate.
3. Which term of the disjunction is to replace the surrogate.

Obviously criteria are penalties obtained by anticipating the first dual iteration, pseudocosts and user supplied priorities.

3.1 Other Criteria

Rado (1966) suggests a maxmin criterion. For each disjunction, note the term which has the smallest "infeasibility" and let this be (by definition) the infeasibility of the disjunction. Arbitrate on the disjunction which has the largest infeasibility. The infeasibility is defined as $\sum_{j=1}^n a_j x_j - b$ for a constraint of form $\sum_{j=1}^n a_j x_j \leq b$ and analogously for other forms.

We suggest a surrogate criterion.

1. Arbitrate on the infeasible disjunction whose surrogate has the highest non-zero shadow price.
2. If no disjunction is chosen in (1), arbitrate on the infeasible disjunction whose surrogate has the smallest slack.
3. In either case select the term with the smallest infeasibility gap.

For some problems (1 and 2) this criterion seems to be effective, evidently giving a good measure of the importance of a disjunction. This criterion appears to dominate the maxmin criterion. Dimensional considerations suggested multiplying the shadow price by the infeasibility, but this worsened performance.

4. IMPLEMENTATION AND RESULTS

The conventional and disjunctive algorithms were compared by coding (in FORTRAN 77 on a VAX/750) the Land-Doig algorithm (Land and Powell 1973) with MINOS 4.0 (Murtagh and Saunders 1977) being used to solve subproblems. Both programs use MPS input format except that the disjunctive program reads row cards of type "OR" and "AN" to define logical constraints.

2.3.4 Scenarios

To describe scenarios one needs a data structure that expresses inter-period dependencies. This is best developed as a description of the distribution of a process vector in the periods, $t = 1, \dots, T$, just as one may describe a stochastic process in probability theory. We consider the random entries of $(c_t, b_t, A_{ts} : s \leq t)$ as states of a process vector φ_t , for each time $t = 1, \dots, T$. Given the corresponding (finite dimensional) joint distributions of this process φ , Kolmogorov's construction yields a probability measure P , termed the *process distribution*, on the space Ω of trajectories. Thus, in general, we have the alternatives of describing the distribution of the stochastic process φ in joint or conditional state distribution form, or as a process distribution over trajectories.

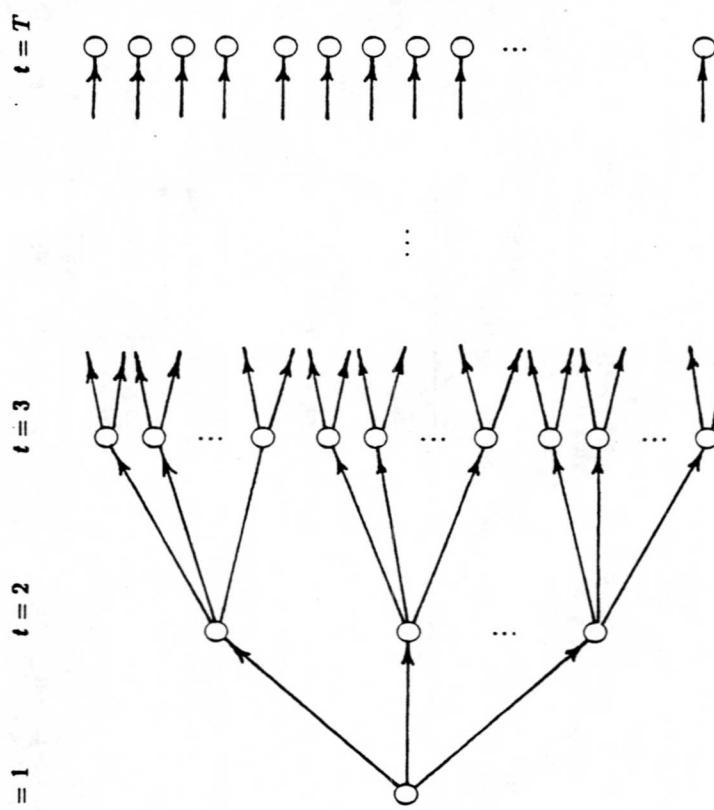


Figure 1. Event tree representation of scenarios

More specifically, with the stochastic process φ is associated a filtration $\{\mathcal{F}_t : t = 1, \dots, T\}$, where for each t the sigma algebra \mathcal{F}_t consists of subsets of Ω termed events determined by the history of the process φ up to time t , and $\mathcal{F}_t \subset \mathcal{F}_{t+1}$ for

BLOCKS	SUB
BL_BLOCK1	PERIOD2
COL1	ROW6
COL2	ROW8
BL_BLOCK2	PERIOD2
RHS	ROW6
RHS	ROW8

Here we have identified two blocks, each a 2-vector, **BLOCK1** and **BLOCK2** whose distributions must be computed by a subroutine.

Linear Transformations. These are blocks whose distribution is computed as a linear transformation of another random vector with independent components, i.e.,

$$v = Hv$$

where H is a matrix and v and u are random vectors. The vector v is the block whose distribution is desired; the vector u has independently distributed components of standard type, e.g., normal. We first identify the block as in the subroutine case, then the (marginal) distribution of each (independent) component of u followed immediately by the corresponding column of H .

BLOCKS	LINTR
BL_BLOCK	PERIOD2
COL1	ROW8
COL3	ROW6
RV_U1	NORMAL
COL1	μ
COL3	h_{11}
ROW6	h_{21}
RV_U2	UNIFORM
COL1	a
COL3	h_{12}
ROW6	h_{22}
RV_U3	CONSTANT
COL3	C

This example illustrates the file structure. In this case

$$\begin{aligned} \text{COL1/ROW8} &= h_{11} \cdot N(\mu, \sigma^2) + h_{12} \cdot U(a, b) \\ \text{COL3/ROW6} &= h_{21} \cdot N(\mu, \sigma^2) + h_{22} \cdot U(a, b) + C. \end{aligned}$$

General multivariate normal [8] and multigamma distributions [13] can also be treated in this way. Note that the "names" U_1 , U_2 and U_3 are irrelevant and may be left blank.

The conventional version chooses a variable and direction of arbitration by multiplying the distance from the nearest integer by the variable's objective function coefficient (taken to be 1 if it is in fact zero). The variable for which the absolute value of this product is highest is arbitrated, initially to its nearest value.

The disjunctive algorithm builds the surrogates and applies the algorithm described with the surrogate criterion. Occasionally the maximum criterion is used, especially to test a likely solution. It was expedient to store the logical constraint structures, the generated surrogates and much other information in indexed files.

The results are in Table 1.

Problem 1, assumed to be available to the reader, illustrates some of the pros and cons of the disjunctive approach. It is relatively simple to formulate in disjunctive terms, extra variables S_{it} , the discounted royalty actually paid on mine i in year t are required but William's binary variables are not needed. The constraints are:

$$\begin{aligned} x_{it} &\leq M_i && \text{all } t, t \\ S_{it} &\leq R_{it} && \text{all } t, t \\ S_{it} &> R_{it} \text{ OR } x_{it} = 0 && \text{all } t, t \\ \sum_{t=1}^4 x_{it} &= 0 && \text{all } t \\ \sum_{t=1}^4 q_t x_{it} &= p_t q_t && \text{all } t \\ \sum_{t=1}^4 x_{it} &= q_t && \text{all } t \\ \max \sum_{t=1}^4 \sum_{i=1}^5 -S_{it} + \sum_{t=1}^4 l_t q_t &&& \end{aligned}$$

This formulation is correct and perhaps more natural, but does not give the tightest possible relaxation. It is desirable to add the constraints:

$$dS_{it} > S_{it+1} \quad \text{all } t, \text{ all } t < 5$$

where d is the discount factor. That done, the disjunctive algorithm compares well with the conventional approach.

Problem 3 demonstrates that the disjunctive algorithm sometimes performs much worse than the conventional algorithm.

5. CONCLUSION

The disjunctive algorithm shows some advantages (simpler formulation, a smaller matrix, a smaller tree and less CPU time) on some kinds of problem. Comparisons of performance might be affected, e.g. by tolerances.

The disadvantages are:

1. In general, nodal problems are formed by altering the matrix. This implies that each subproblem must start with a reinversion. If, as is common, the terms of a disjunction are bounds, arbitration can be (and is) expressed by altering variable bounds in which case reinversion is not needed. It should be noted that all subproblems in both programs start with a reinversion.
2. Generating, storing and altering the constraints is much more difficult and time consuming than retaining the values of arbitrated variables.

It is intended to speed up both programs (especially by removing unnecessary reinversions) and do more benchmarking. Suitable test problems would be much appreciated.

A longer paper which outlines some extensions is available from the author.

6. REFERENCES

- RADO, F. (1966), "Linear Programming with Logical Conditions", Matekon 3, 52-56.
- LAND, A.H. and S. POWELL (1973), Fortran Codes for Mathematical Programming, John Wiley and Son, New York.
- MURTAGH, B.A. and M.A. SAUNDERS (1977), MINOS 4.0 User's Guide, Technical Report SOL 77-9, Department of Operations Research, Stanford University, California.
- SHERALDI, H.D. and C.M. SHETTY (1980), Optimization with Disjunctive Constraints, Springer-Verlag, Berlin.
- WILLIAMS, H.P. (1978), Model Building in Mathematical Programming, John Wiley and Sons.

in a similar fashion to the normal, using the standard descriptors as presented in, for example, Raiffa and Schlaifer [16]. An adjustment to other intervals could be effected within the framework of the linear transformations described below.

Subroutine. Some random entries may have distributions that are computed by subroutines, for example, empirical distributions which are discretely distributed but whose values may be randomly generated by user-supplied computer codes.

```
INDEP      SUB      PERIOD2
          COL1    ROW8    blank
```

This example indicates that the user must access a subroutine to generate an appropriate distribution for the entry COL1/ROW8.

2.3.3 Blocks

Blocks may be regarded as mutually independent random vectors. We provide for three distribution types: *discrete*, *subroutine*, or *linear transformation*. As in the independent case, blocks with common distribution types are grouped in the same section under a header line.

Discrete. The "values" of a block are actually vectors of values of the entries that make up the block, and to each value of a block there corresponds a probability. We need two sorts of data lines to describe a block. The first line, distinguished by a BL in the code field, gives the name of the block, the name of the period in which the block is realized, and the probability that the block assumes a given vector value; the following lines identify which entries of the block assume which value.

BLOCKS	DISCRETE
BL BLOCK1	PERIOD2 0.5
	COL1 ROW6 83.0
	COL2 ROW8 1.2
BL BLOCK1	PERIOD2 0.2
	COL2 ROW8 1.3
BL BLOCK1	PERIOD2 0.3
	COL1 ROW6 84.0

One needs to record only those values that change. We adopt the convention that the first statement of the block is the basis from which all changes are computed. (Thus zero values must be stated explicitly.) In this example the block, called BLOCK1, is the 2-vector made up of the entries COL1/ROW6 and COL2/ROW8. It takes values (83.0, 1.2) with probability 0.5, (83.0, 1.3) with probability 0.2, and (84.0, 1.2) with probability 0.3.

Subroutine. The user accesses a subroutine to compute the distribution of the block consisting of the listed entries.

2.3.2 Independent

Independent random variables are easily treated. We provide facilities for identifying entries that are distributed as discrete, uniform, beta, gamma, normal and log-normal; certainly other distributions may be considered. The INDEP header line is repeated for each new distribution type; entries with the same type are listed together following the appropriate header. The keyword in the second word field of the header identifies the distribution. The data lines indicate the entry by column and row in the first two name fields, and the distribution parameters are entered in the first and second numeric fields.

Discrete. For each discretely distributed entry one must specify the values and corresponding probabilities. The first two name fields identify the entry, and the first two numeric fields are the value field and probability field respectively. The intervening third name field contains the name of the period in which the random variable is realized (this information is ignored by the input routine but is useful to have made explicit for data consistency checking).

INDEP	DISCRETE					
COL1	ROW8	6.0	PERIOD2	0.5		
COL1	ROW8	8.0	PERIOD2	0.5		
RHS	ROW8	1.0	PERIOD2	0.1		
RHS	ROW8	2.0	PERIOD2	0.5		
RHS	ROW8	3.0	PERIOD2	0.4		

In this example the entry COL1/ROW8 takes value 6.0 with probability 0.5 and 8.0 with probability 0.5; and the righthand side of ROW8 takes values {1.0, 2.0, 3.0} with probabilities {0.1, 0.5, 0.4} respectively. Of course the probabilities associated with an entry must total one.

Uniform. The endpoints of the interval are the only relevant parameters for uniformly distributed entries. These are entered into the first two numeric fields; the third name field is blank.

INDEP	UNIFORM					
COL1	ROW8	8.0	PERIOD2	9.0		

In this example the random entry COL1/ROW8 is uniformly distributed over the interval [8.0, 9.0].

Normal. The normal distribution is specified by mean μ and variance σ^2 in the first two numeric fields.

INDEP	NORMAL					
COL1	ROWS	μ	PERIOD2	σ^2		

Beta, Gamma, Lognormal. The standard beta on $[0, 1]$, gamma on $[0, \infty)$, log-normal on $[0, \infty)$ are two-parameter families of distributions and may be handled

RUNNING THE NATO WORKSHOP FOR COAL

Sverre Storøy

Department of Informatics, University of Bergen, Norway

Stein W. Wallace

Chr. Michelsen Institute, Bergen, Norway

Now, as the workshop is history, and our file has been closed by NATO, it seems to be time to share some of our experiences with the readers of COAL Newsletter. This is not going to be an encyclopaedia of how to run a workshop, but hopefully we can give some useful advice.

For those who did not take part in the event, let us briefly mention that we are talking about a workshop with limited participation (about 40), and where the participants were invited based on submitted abstracts. The workshop ended up being supported as a NATO Advanced Research Workshop.

Below are three sections. The first indicates the amount of time needed to plan and run the workshop, the second which things went wrong, and the third discusses aspects of the workshop that we think worked nicely. Hopefully all three sections can be of some help to people in a situation similar to ours.

How much time did it take to plan and run the workshop? Since the workshop was run at Chr. Michelsen Institute, a private independent, non-profit research institute, some of the procedures of such an institution help us in evaluating the actual time spent on planning. Based on very detailed time-sheets, we are able to estimate the total number of hours spent on planning and running the workshop to about 600, or about 1/3 of a man-year. This includes everything from making an initial contact with COAL, via applying twice to NATO, sending out the organization of the event itself and cleaning up afterwards. It is our firm belief that if we had to do it again, we would still use about the same amount of time. There are some errors we would not do again (see below), but new errors would certainly show up.

Errors we made in the planning. There are clearly several errors of minor importance that were made during the planning process. Below follows a list of errors that we hope it will be useful to think about also for other who wish to run a workshop.

Call-for-papers. As pointed out above, participants were invited based on submitted extended abstracts. Hence, in the call-for-papers we asked people to send us such abstracts together with a registration form. At this point we made what we believe to be our major error.

In this example: Columns COL1 through COL5 are PERIOD1 decision variables and COL6 and COL7 are PERIOD2 variables; rows ROW1 and ROW2 are PERIOD1 constraints and ROW3 through ROW18 are PERIOD2 constraints. All remaining rows and columns belong to PERIOD3.

Other possible keywords on the PERIODS line are **NETWORK** for pure network problems and **MIXED** for coupled LP/network problems. These are explained in some more detail in sections 3.2 and 4, respectively.

2.3 Stock File

In the **stock** file the distributions of the random variables are specified. As mentioned, we consider three varieties of distributions: **independent**, **blocks**, and **scenarios**. Each type will be treated in separate sections of this file; each section consists of a header line followed by data lines.

Stock file – header lines

1. **STOCK** – informative. Identifies a new problem with a give name in the second word field.
2. **INDEP** section – specifies the distribution of all independent random entries in separate sections for each type.
3. **BLOCKS** section – specifies the joint distribution of all dependent random entries in separate sections for each type.
4. **SCENARIOS** section – specifies the scenarios.
5. **ENDATA** – informative. End of problem data.

2.3.1 A note on distributions

The purpose of the stock file is to give the user the information needed to compute with the random variables. In many applications the distributions are discrete or discrete approximations of (absolutely) continuous distributions; thus the user needs, ultimately, to know what value the random variable takes and with what probability. The discrete case is straightforward—this information may be explicitly provided in the stock file and then stored in appropriate data structures by the user. In the continuous case users may have their own discretization scheme and may need only to know the parameters and type of the continuously distributed random variables. Such data is easily provided; however, users must then process it themselves to obtain a discrete approximation. Finally there are cases where the random variables may be accessed only through a **user-supplied subroutine**—for example the output of a random number generator of nonstandard type. Alternatively, the user may be able to compute directly with certain continuous distributions and may build approximations to more general distributions based on them—for example the piecewise linear and piecewise quadratic distributions investigated by Wets [17] and Birge and Wets [2]. This information is easily transmitted using the various data structures described below.

Core file – example

```

NAME      problem name
ROWS
N   OBJ
L   ROW1
E   ROW2
.....
COLUMNS
COL1    ROW1    value
        ROW3    value
        ROW4    value
COL2    ROW1    value
        ROW2    value
RHS     ROW1    value
        ROW2    value
.....
BOUNDS
LO BND  COL1    value
        .....
RANGES
        .....
ENDATA

```

If an entry is *random* then the *value* field should contain a non-zero number (which may or may not be meaningful). This number *must not be omitted* from the core file. Integer variables may be indicated by using delimiters as described in the MPSX/MIP documentation [7] for those users who want to use mixed integer programming techniques.

2.2 Time File

The *time file* contains the information needed to specify the dynamic structure of the problem. It indicates which rows and columns (i.e., elements of the decision vector *z*) are to be identified with which period. The first line identifies it as a time file and gives a name to the problem. The next header line consists of a single word PERIODS in the first name field, and contains the keyword LP in the second name field to identify the problem as a pure LP. The first two name fields of the data lines identify the beginning row and column names for each period with the corresponding period name in the third name field.

Time file – example

```

TIME      problem name
PERIODS   LP
          PERIOD1
          PERIOD2
          PERIOD3
COL1     ROW 1
COL6     ROW 3
COL8     ROW19
ENDATA

```

An example illustrates the problem. We receive an abstract by Professors A, B and C together with a registration form from B. The abstract looks interesting, and so it is accepted. Now, how many participants do we have? Remember that we have a limitation on the number of participants, not on the number of presentations. Of course, people who sent us such abstracts had different ideas. Some thought that with the abstract accepted, all three people would automatically be invited, others took it for granted that only those that had sent registration forms wanted to participate (and everybody thought that their interpretation was obvious). We ended up sending letters to all authors of papers with more than one author asking if they wanted to participate.

So what should have been done was to distinguish clearly between authors, participants and abstracts. One should probably also let the authors give a priority amongst themselves. (What would you do if you received a marvellous abstract with 25 authors?)

NATO application. We ended up with NATO money after having applied twice. The result was that we ran short on time for doing publicity for the workshop. We have been criticized by many people for not getting the information out. We accept the criticism, but wish to point out that our mistake was to apply for money from NATO as if we would have a final answer after our first application. Instead we were encouraged to apply again, which we did. That cost us another four months, which meant a lot from a publicity viewpoint.

So, if you wish to apply for NATO funding, and you think that what you need is a final answer in November, subtract four months (you can apply three times a year) and go for July instead. To have an answer in July you will have to apply in April. That way you should be quite certain of a final response in November.

Things that went right. The purpose of this section is not to list those things that went smoothly, but to give a few ideas about things that we believe could be useful for others to think about.

As mentioned, this was a workshop, and somehow that had to be reflected in the structure of the meeting. We chose to invite five key-note speakers, one for each day of the workshops. They were told to see the workshop's major theme from different perspectives, and present their views in such a way that it would provoke comments and discussions. The idea was not to present "ordinary" tutorials. The key-note speakers were given the first 90 minutes of the morning sessions, and the presentations were followed by 45 minutes of plenary discussions. To the extent that it was possible, the technical papers presented during the rest of the day were related to that day's key-note presentation. There were no parallel sessions.

The above structure is, of course, in no way revolutionary. Still, we felt that it worked so well, that it is worth being thought about also by other organizers.

trust that many problems will become available using the basic elements to the fullest extent—with tailored modifications only when absolutely necessary.

2. Standard Format for Linear Programs

2.1 Core File

CALENDAR

1988

August 1 Paper deadline, Mathematical Programming Series B special issue on large-scale optimization (see p. 30).

August 24-26 Seoul, Korea: First Conference of the Association of Asian-Pacific Operational Research Societies within IFORS - APORS '88.
Information: IFORS Secretary & APORS '88 Org. Committee, Dept. of Ind. Eng., College of Engineering, Seoul National Univ., Seoul, Korea 151.

Aug. 29 - Sept. 2 Tokyo, Japan: 13th INTERNATIONAL SYMPOSIUM on MATHEMATICAL PROGRAMMING.

Oct. 10-14 Rio de Janeiro, Brazil: Workshop on Mathematical Programming, Catholic University of Rio de Janeiro, Co-sponsored by MPS (see p. 31).

Oct. 17-21 Rio de Janeiro, Brazil: ALIO (Latin Iberian American Assoc. of O.R.) IV Latin-Iberian-American Congress on O.R. and Systems Eng.
Information: IFORS Secretary & Nelson Maculan, COPPE & Inst. de Mathem., Univ. Federal do Rio de Janeiro, Caixa Postal 68501, Rio de Janeiro, RJ, Brazil.

The core file is sketched only briefly since it closely follows the MPSX standard [6]. The core file consists of sections introduced by header lines. Data lines follow the headers. We assume that all appropriate dimensioning has been done before the files are read (for example in a file similar to the SPECS file for the MINOS program [12]).

A data line is divided into six fields: three name fields, two numeric fields and one code field.

Data line for LP

- columns 2 and 3: code field
- columns 5-12: first name field
- columns 15-22: second name field
- columns 25-36: first numeric field
- columns 40-47: third name field
- columns 50-61: second numeric field

A name is treated as a character string and may contain any ASCII symbol. Only numbers with decimal point, or in scientific notation, may appear in numeric fields.

Core file sections for LP

1. NAME – starts the input file. The second word field is used to identify the problem.
2. ROWS section – each data line specifies the names of the objective c and rows of the matrix A in the first name field, and the type of constraint (E, L, G, N) in the code field. The list of row names must be in order from first period to last, preceded by the objective name(s).
3. COLUMNS section – each data line specifies the column names and the nonzero values of c and A. This must be done in column order.
4. RHS section – data lines specify nonzero entries of the righthand side b.
5. BOUNDS (optional) – data lines specify the bound, u and l, using the codes L0 or UP in the code field.
6. RANGES (optional) – cf. the MPSX standard [6].
7. ENDATA – informative. End of problem data.

purely deterministic problem and create an input file following the MPSX convention, ignoring (non-random) zero entries. This file will identify an objective vector c , upper and lower bounds u and l , a right hand side b , and a block lower-triangular matrix A , all expressed in the usual column-row format; we call this the *core file*.

Next we note the period structure of the problem, that certain decisions $x_t \in \mathbb{R}^n$ are made at times $t = 1, \dots, T$. Here it is necessary only to specify which rows and columns from the core file correspond to which periods. It is most simply done by indicating the beginning column and row for each period t . This is done in the *time file*. Note that such a system relies on the proper sequencing of the core file—we require that the list of row names is in order from first period to last period and that the block lower-triangular matrix A has been entered in column order: first period columns first, and last period columns last.

Finally there remains the specification of the distributions of the random entries; this takes place in the *stock file*. The simplest case occurs when all random entries are mutually *independent*—one merely indicates by keywords which entries are distributed as discrete, uniform, beta, gamma, etc., and supplies the appropriate parameters. One may even use the entries in the core file to supply some of the parameters. We consider two general types of dependency among the random entries: *blocks* and *scenarios*. A block is a random vector whose realizations are observed in a single, fixed period. A scenario is a more general type of stochastic structure which models dependencies across periods. Following Lane and Hutchinson [11], we visualize scenarios as paths in an event tree. Each path corresponds to a particular sequence of events through time, and is assigned a probability that is the product of the conditional probabilities of the separate events.

The organization of the data files is similar to the MPSX format [6; pp. 199–209]. Each data file contains a number of *sections*, some of which are optional. A *header line*, or *header*, marks the beginning of each section and may contain *keywords* to inform the user that the data to follow should be treated in a special way. Each header line is divided into two fields delineated by specific columns.

Header line

- columns 1 through 14: first word field
- columns 15 through 24: second word field

Most sections contain *data lines*. These are differently arranged for linear programs than for networks and each version will be described in the appropriate sections. Data lines are distinguished by a blank in the first column; the first word of a header line must, therefore, begin with a non-blank character. Finally, *comment lines* are indicated by an asterisk (*) in the first column and may appear anywhere. We close this section with a comment to potential users. The header lines are a powerful device that permits the expression of a wide variety of problem types, however, one should not exploit it by tailoring a format convenient for one's own peculiar taste in test problems. That is definitely not in the spirit of our proposal! Rather we hope that this proposal offers sufficient flexibility to be useful and we

1989

July 4-6

Williamsburg, VA, U.S.A.: Impact of Recent Computer Advances on Operations Research, organized by the Computer Sciences Technical Section of ORSA.

Information: Prof. Ramesh Sharda, College of Business Administration, Oklahoma State University, Stillwater, OK 74078, U.S.A.

April 10-13

Cambridge, U.K.: IFORS Specialized Conference on Operational Research and the Social Sciences, organized by the Operational Research Society.

Information: ORS - Neville House, Waterloo St., Birmingham, B2 5TX, U.K.

July 23-26

Osaka, Japan: TIMS XXIX/Osaka '89. Information: TIMS XXIX, TIMS, 290 Westminster Street, Providence, RI 02903, U.S.A.

August 29-31

Berlin, GDR: IFAC Symposium on Large Scale Systems: Theory and Applications.

Information: Prof. Dr. Dietrich Ohse, Fachbereich Wirtschaftswissenschaften, Johann Wolfgang Goethe Univ., Postfach 111932, D-6000 Frankfurt/Main, West Germany.

CALL FOR PAPERS

where the functions Q_1, Q_2, \dots, Q_T are defined recursively:

$$Q_2(\mathbf{x}_1) = \min\{c_1 \mathbf{x}_2 + E_3 Q_3(\mathbf{x}_1, \mathbf{x}_2)$$

subject to $\mathbf{x}_2 \in \mathbb{R}^{n_2}$

$$\begin{aligned} \mathbf{t}_1 &\leq \mathbf{x}_1 \leq \mathbf{u}_2 \\ A_{31}\mathbf{x}_1 + A_{32}\mathbf{x}_2 &= b_3 \end{aligned};$$

$$Q_3(\mathbf{x}_1, \mathbf{x}_2) = \min\{c_3 \mathbf{x}_3 + E_4 Q_4(\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3)$$

subject to $\mathbf{x}_3 \in \mathbb{R}^{n_3}$

$$\mathbf{t}_3 \leq \mathbf{x}_3 \leq \mathbf{u}_3$$

$$A_{31}\mathbf{x}_1 + A_{32}\mathbf{x}_2 + A_{33}\mathbf{x}_3 = b_3;$$

If you have a suitable paper for such an issue you are invited to submit it to one of the editors:

A. R. Conn
 Department of Combinatorics and Optimization
 Faculty of Mathematics
 University of Waterloo
 Waterloo, Ontario N2L 3G1
 Canada
 Tel: 519-885-4458
 E-mail: arconn@water.math.uwaterloo.ca
 arconn@water.math.uwaterloo.edu

N. I. M. Gould
 Computer Science and Systems Division
 A.E.R.E. Harwell
 Oxfordshire OX11 ORA
 U.K.
 Tel: 235-24141 ext. 3357
 E-mail: nimgould@water.math.uwaterloo.ca
 nimgould@water.math.uwaterloo.edu

Ph. L. Toint
 Department of Mathematics
 Facultes Universitaires Notre Dame de la Paix
 Rue de Bruxelles, 61
 B-5000 Namur, Belgium
 Tel: 32-81-229061 ext. 2592
 E-mail: phoint@bmndp10.bitnet

The deadline for submission is August 1, 1988 for the issue that is to be published in 1989. Late submissions, an excess of submissions etc. would automatically be considered for Mathematical Programming Series A, unless the author wishes otherwise.

All entries of the matrices A_t , and vectors: c_t , \mathbf{t}_t , \mathbf{u}_t , b_t may be random (although in practice all but a few entries will be deterministic). The indices $t = 1, \dots, T$ signify the periods of the problem; to each period t there corresponds a decision vector $\mathbf{x}_t \in \mathbb{R}^{n_t}$. The lower block-triangular constraint system expresses the typical feature of these problems—the decisions of the prior periods constrain the decision of the current period explicitly (since those decisions are known) but the decision of the current period is affected only implicitly by the feasibility and costs of possible future (recourse) decisions.

The proposed format is most easily understood by considering the problem (MP) in stages of gradually increasing levels of detail. First we regard (MP) as a

0. Introduction

WORKSHOP ON MATHEMATICAL PROGRAMMING

CATHOLIC UNIVERSITY OF RIO DE JANEIRO, BRAZIL

OCTOBER 10-14, 1988

The desire to solve stochastic optimization problems as more realistic models than deterministic formulations for decision making began in the early days of linear programming, see Dantzig [3] for example. As evidenced by recent volumes, Prékopa and Wets [14] and Ermoliev and Wets [5], there is a wide body of active research into numerical algorithms. However, these efforts have tended to be directed towards specialized types of problems resulting in a potpourri of numerical codes, problem formulations and data sets that are not comparable or even mutually compatible. The development of general purpose codes suitable for industrial application is hampered by the lack of a comprehensive set of test problems in a standard format to compare performance and challenge competitors. In this paper we present our ideas on what we hope will become the nucleus of a standard problem format for multistage stochastic linear programs.

The present contribution is an extension, simplification, and refinement of the ideas in Edwards, et al. [4]. The spirit of the two proposals is identical: (a) to use the MPSX convention for file formats; (b) to allow originally deterministic problems to be changed to stochastic versions; (c) to permit a wide variety of stochastic dependencies; and (d) to allow new options to be added. Two key aspects of the original proposal are retained—the use of separate files to specify parameters related to random variables and the use of “header lines” to express and organize the relevant parameters.

After a statement of the problem in the form we shall consider it, we present in Section 2 our proposed input format. In Section 3 we present an extension of the standard format to cover multistage stochastic network problems using the NETGEN format [10], and in the final section we set out our recommendations for mixed stochastic network and linear programs.

The collection of test problems is an ongoing enterprise in which readers are encouraged to participate. Some examples, augmenting those already presented in King [9] and illustrating the standard problem format, are available in computer accessible form.

1. Problem Statement

A general form of the multiperiod stochastic linear program is:

$$\begin{aligned} \text{minimize } & c_1 x_1 + E_1 Q_1(x_1) \\ \text{subject to } & x_1 \in I\!\!R^n \\ & l_1 \leq x_1 \leq u_1 \\ & A_1 x_1 = b_1, \end{aligned}$$

MAIN THEMES:

COMBINATORIAL OPTIMIZATION
NONDIFFERENTIABLE OPTIMIZATION
PROJECTIVE ALGORITHMS
APPLICATIONS

PROGRAM COMMITTEE:

CELSO RIBEIRO (PUC/RJ, BRAZIL), CHAIRMAN
MICHEL BALINSKI (ECOLE POLYTECHNIQUE, FRANCE)
MARTIN GROTSCHEL (UNIVERSITAT AUGSBURG, GERMANY)
NELSON MACULAN (COPPE AND IM/UFRJ, BRAZIL)
PHILIPPE MAHEY (PUC/RJ, BRAZIL)
WILLIAM PULLEYBLANK (UNIVERSITY OF WATERLOO,
CANADA)

INVITED LECTURERS:

J. ARAOZ, M. BALINSKI, F. BARAHONA, R.A.
CUNINGHAME-GREEN, J. FERLAND, C. GONZAGA,

M. GROTSCHEL, P. HAMMER, P. HANSEN, J. B.

HIRIART-URRUTY, K.C. KIWIEL, B. KORTE,

F. LOUVEAU, F. MAFFIOLI, N. MACULAN, P.

MAHEY, M. MINOUX, V.H. NGUYEN, M. PADBERG,

W. PULLEYBLANK, C. RIBEIRO, R.T. ROCKAFELLAR,

J. SPINGARN, M. TODD, P. TOTH, A. WEINTRAUB,

CATHOLIC UNIVERSITY OF RIO DE JANEIRO, BRAZIL
MATHEMATICAL PROGRAMMING SOCIETY

INFORMATION AND MAIL:

PROF. CELSO C. RIBEIRO
CATHOLIC UNIVERSITY OF RIO DE JANEIRO
DEPARTMENT OF ELECTRICAL ENGINEERING
GAVEA - CAIXA POSTAL 38063
RIO DE JANEIRO 22452

BRAZIL

PHONE: (55)(21) 529-9334/529-9336/
529-9246/529-9397
TELEX: (021) 31048

A STANDARD INPUT FORMAT FOR MULTIPERIOD STOCHASTIC LINEAR PROGRAMS

COAL OBJECTIVES

The Committee on Algorithms is involved in computational developments in mathematical programming. There are three major goals: (1) ensuring a suitable basis for comparing algorithms, (2) acting as a focal point for computer programs that are available for general calculations and for test problems, and (3) encouraging those who distribute programs to meet certain standards of portability, testing, ease of use and documentation.

J.R. Birge

*Department of Industrial and Operations Engineering
University of Michigan, Ann Arbor, USA*

M.A.H. Dempster

*Department of Mathematics, Statistics and Computing Sciences
Dalhousie University, Halifax, Canada
and Balliol College, Oxford, England*

H.I. Gassmann

*School of Business Administration
Dalhousie University, Halifax, Canada*

E.A. Gunn

*Department of Industrial Engineering
Technical University of Nova Scotia, Halifax, Canada*

A.J. King

*International Institute for Applied Systems Analysis
Laxenburg, Austria*

S.W. Wallace

Chr. Michelsen Institute, Bergen, Norway

NEWSLETTER OBJECTIVES

The newsletter's primary objective is to provide a vehicle for the rapid dissemination of new results in computational mathematical programming. To date, our profession has not developed a clear understanding of the issues of how computational tests should be carried out, how the results of these tests should be presented in the literature, or how mathematical programming algorithms should be properly evaluated and compared. These issues will be addressed in the newsletter.

ABSTRACT

Data conventions for the automatic input of multiperiod stochastic linear programs are described. The input format is based on the MPSX standard and is designed to promote the efficient conversion of originally deterministic problems by introducing stochastic variants in separate files. A flexible "header" syntax generates a useful variety of stochastic dependencies. An extension using the NETGEN format is proposed for stochastic network programs.

**COMMITTEE ON ALGORITHMS OF THE
MATHEMATICAL PROGRAMMING SOCIETY**

CHAIRMAN	EDITOR	CO-EDITOR
Jan Telgen Van Dien+Co Organisatie Churchilaan 11 3527 GV Utrecht The Netherlands	Robert R. Meyer Computer Sciences Dept. University of Wisconsin Madison WI 53706 USA	Jens Clausen DIKU University of Copenhagen Sigurdsgade 41 DK-2200 Copenhagen Denmark

MEMBERS

Paul T. Boggs
Center for Applied Mathematics
National Bureau of Standards
Gaithersburg MD 20899
USA

David M. Gay

AT&T Bell Laboratories

Murray Hill NJ 07974
USA

James K. Ho

Management Science Program

University of Tennessee
Knoxville TN 07974
USA

Karla L. Hoffman

Center for Applied Mathematics

National Bureau of Standards
Gaithersburg MD 37996
USA

Richard H. F. Jackson

Center for Applied Mathematics

National Bureau of Standards
Gaithersburg MD 20899
USA

Gautam Mitra

Brunel University

Dept. of Mathematics and Statistics
Uxbridge, Middlesex UB8 3PH
England

James B. Orlin

Sloan School of Management

MIT
Cambridge, MA 02139
USA

Ronald R. Rardin
School of Industrial and Sys. Eng.
Purdue University
West Lafayette IN 47907
USA

Klaus Schittkowski

Mathematisches Institut

Universität Bayreuth

D-8580 Bayreuth

BRD

Robert B. Schnabel

Dept. of Computer Science

University of Colorado

Boulder CO 80309
USA

William R. Stewart

Sch. of Business Administration

College of William and Mary

Williamsburg VA 23185
USA

Philippe L. Toint

Dept. of Mathematics

University Notre Dame de la Paix

Namur, Belgium

Stein W. Wallace

Chr. Michelsen Institute

N 5036 Fantoff
Norway

EX OFFICIO MEMBERS

Jan Karel Lenstra
Chairman Executive Committee MPS

CWI
Postbus 4079
1009 AB Amsterdam
The Netherlands

Michel L. Balinski
Chairman MPS Council
Ecole Polytechnique
5 Rue Descartes
75005 Paris
France



Mathematical Programming Society
Committee on Algorithms
Newsletter

NO. 17	JENS CLAUSEN	EDITORS
DECEMBER 1987	ROBERT R. MEYER	
CONTENTS		
A Standard Input Format for Multiperiod Stochastic Linear Programs		1
J. R. BIRGE, M. A. H. DEMPSTER, H. I. GASSMANN, E. A. GUNN, A. J. KING, S. W. WALLACE		
An Algorithm for Disjunctive Programming Problems		20
N. BEAUMONT		
Running the NATO Workshop for COAL		26
S. STORØY, S. W. WALLACE		
Calendar		28
Call for Papers		30
Workshop on Mathematical Programming		31

ROBERT R. MEYER
UNIVERSITY OF WISCONSIN-MADISON
COMPUTER SCIENCES DEPARTMENT
1210 WEST DAYTON STREET
MADISON, WISCONSIN 53706